

Lab writeups individual. (Due last day of class.)

Professional lab report, 10-20 pages procedure and example data.

To do: Bloch equations

Total NMR Hamiltonian?
And/or spin operators

Recall,

$$\frac{dM_x}{dt} = \omega_0 M_y - \overset{\text{Relaxation}}{\downarrow} \frac{M_x}{T_2}$$

$$\frac{dM_y}{dt} = -\omega_0 M_x - \frac{M_y}{T_2}$$

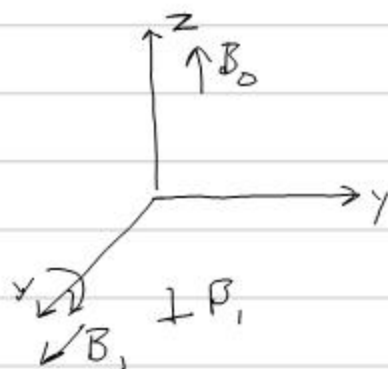
$$\frac{dM_z}{dt} = 0 - \frac{M_z - M_0}{T_1} \leftarrow \text{equilibrium magnetization}$$

Add a \perp B_1 field.

Had components like $\gamma (\vec{M} \times \vec{B})$

$$\omega_0 = \gamma B$$

$$\omega = \gamma B_1$$



$$B_{1x} = B_1 \cos(\omega t)$$

$$B_{1y} = B_1 \sin(\omega t)$$

Complete Bloch Equation

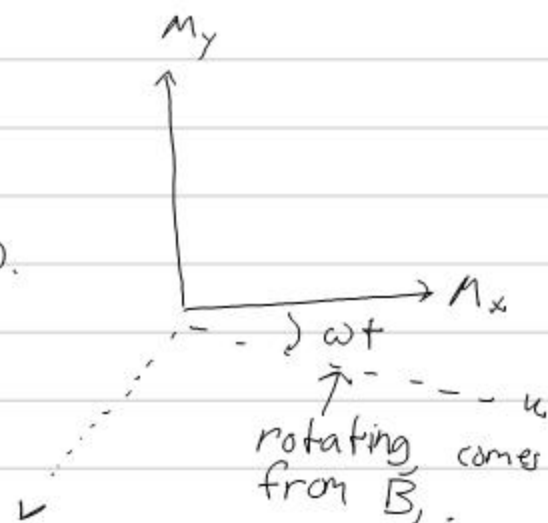
$$\frac{dM_x}{dt} = \gamma(-M_y B_0 + M_z B_1 \sin(\omega t)) - \frac{M_x}{T_2}$$

$$\frac{dM_y}{dt} = \gamma(M_z B_1 \cos(\omega t) - M_x B_0) - \frac{M_y}{T_2}$$

$$\frac{dM_z}{dt} = \gamma(-M_x B_1 \sin(\omega t) - M_y B_1 \cos(\omega t)) - \frac{M_z - M_0}{T_1}$$

From some algebra

Like a frequency
offset $\omega_0 - \omega$.



1) Slow passage case - old time CW NMR

• B_1 is negligible

→ sweep spectrum, record absorptive

& dispersive signals:

• First case of nuclear induction: rotating magnetic fields led to signal in a coil

$$u = M_0 \left(\frac{\gamma B_1 T_2^2 (\omega_0 - \omega)}{1 + T_2^2 (\omega_0 - \omega)^2 + \gamma^2 B_1^2 T_1 T_2} \right)$$

$$v = M_0 \left[\frac{1 + T_2^2 (\omega_0 - \omega)^2}{1 + T_2^2 (\omega_0 - \omega)^2 + \gamma^2 B_1^2 T_1 T_2} \right]$$

u predicts a dispersive signal, v an absorptive one

2. Short pulse experiment, B_1 important

• use a rotating frame of reference

Rotating frame: in a magnetic field, even at equilibrium the spins are precessing at ω_0 .

If your frame of reference also moves around z at ω_0 , " B_0 field disappears."

→ Drop B_0 dependent terms

• rf pulse must be short compared to $T_1, T_2, \gamma B_0$.

• apply along x -axis, so neglect $T_1, T_2, \gamma B_0$ or B_y terms

$$\frac{dM_z}{dt} = -M_y \gamma B_1$$

$$\left. \begin{aligned} \frac{dM_x}{dt} &= 0 \\ \frac{dM_y}{dt} &= M_z \gamma B_1 \end{aligned} \right\} \begin{aligned} M_z &= M_0 \cos(\omega_{1x} t) \\ M_x &= 0 \\ M_y &= M_0 \sin(\omega_{1x} t) \end{aligned}$$

Let $\alpha = \omega_{1x} t$, pulse angle

If $\alpha = 0$, $M_z = M_0$, $M_x = M_y = 0$.
 \rightarrow all magnetization along z

$$\alpha = 90^\circ, M_z(t) = 0, M_y(t) = M_0.$$

At the end of the pulse you go to free precession.

$$M_z(t) = M_0 (1 - e^{-t/T_1})$$

Free Precession

$$M_x(t) = M_0 \cos[(\omega_0 - \omega)t] e^{-t/T_2}$$

$$M_y(t) = M_0 \sin[(\omega_0 - \omega)t] e^{-t/T_2}$$

